

Topic: Function

- a) $f(x) = 64^x + \log x$ find $f\left(\frac{1}{3}\right)$
- b) $f(x) = 16^x - \log_4 x$ find $f\left(\frac{1}{4}\right)$
- c) $f(x) = \frac{x^2+1}{x^3-1}$ find $f(-1)$ & $f\left(\frac{1}{2}\right)$
- d) $f(x) = x^2 + 2x - 5$ find $f(-2)$ & $f(3)$
- e) $f(x) = 3 + \log_4 x$ find $f\left(\frac{1}{4}\right)$

<p>Q1. Find Function is Even or odd</p> <ul style="list-style-type: none"> a) $f(x) = x^3 - 5x + \sin x + x \cos x$ b) $f(x) = \frac{e^x + e^{-x}}{5}$ c) $f(x) = \frac{a^x + a^{-x}}{6}$ d) $f(x) = 3x^4 + x^2 + 5 - 3 \cos x + 2 (\sin x)^2$ e) $f(x) = x^3 + 4x + \sin x$ f) Define Even and odd function with suitable example g) Define implicit function 	<p>Q2. Find value of function</p> <ul style="list-style-type: none"> a) $f(x) = 16^x - \log_2 x$, find $f(1/2)$ b) $f(x) = \log_4 x + 8$, find $f(1/4)$ c) $f(x) = \log_3 x + 64^x$, find $f(1/3)$ d) $f(x) = x^2 + 6x + 10$ find $f(2) + f(-2)$ e) $f(x) = x^3 - x$ find $f(1) + f(2)$ f) $f(x) = x^2 + 5x + 1$ find $f(0) + f(1)$ g) $f(x) = x^2 - x + 1$ find $f(0) + f(3)$ h) $f(x) = x^2 + 6x + 10$ find $f(2) + f(-2)$ i) $f(x) = \frac{x^2+9}{\sqrt{x-3}}$, find $f(4) + f(5)$ j) $f(x) = \frac{x^2+1}{x^3-1}$ find $f(1/4)$
<p>Q3. Show that</p> <ul style="list-style-type: none"> a) $f(x) = x^3 - 5x^2 - 4x + 20$, Show that $f(0) = -2 f(3)$ b) $f(x) = 3x^2 - 5x + 7$ show that $f(-1) = 3 f(1)$ 	<p>Q4. Find missing element value</p> <ul style="list-style-type: none"> a) $f(x) = px^2 + 11$ and $f(-1) = 15$ find p b) $f(x) = ax^2 - bx - 1$, $f(2) = 5$, $f(-2) = 10$ find a and b

Topic: DerivativeQ1. Find dy/dx of following

- a) $y = e^x + a^x + x^a + a^a$
- b) $y = \sin^2(4x)$
- c) $y = \tan^4(x^3)$
- d) $y = \cot [\tan (x^2)]$
- e) $y = \cos(5x^2)$
- f) $y = \sec(4x + \log x)$
- g) $y = \log(\tan x)$
- h) $y = \operatorname{cosec}(x^a + a^a)$
- i) $y = e^{4x} + a^{5x}$
- j) $y = a^{3x} + a^{5a}$

Q2. Find dy/dx of following

- a) $y = e^x \cdot x^3$
- b) $y = e^{5x} \cdot x^7$
- c) $y = \cos^5(3x)$
- d) $y = x^3 \cdot \tan(4x)$
- e) $y = e^{4x} \cdot \cot(6x)$
- f) $y = 5^{3x} \cdot \log(7x)$
- g) $y = \sec(4x) \cdot \operatorname{cosec}(5x)$
- h) $y = \frac{\sec x}{\cos x}$
- i) $y = \frac{\sin 6x}{\cos 5x}$
- j) $y = \frac{x^3}{\log 5x}$
- k) $y = \frac{e^{5x}}{\log x^3}$
- l) $y = \frac{\tan 5x}{\cos}$

Q3. Find dy/dx of following

- a) $x = a(\theta - \sin\theta)$, $y = a(1 - \cos\theta)$
- b) $x = a(\cos t + t \sin t)$, $y = a(\sin t - t \cos t)$
- c) $x = a(\cos^3\theta)$, $y = a(\sin^3\theta)$
- d) $y = 3\sin\theta - 2(\sin^3\theta)$, $x = 3\cos\theta - 2(\cos^3\theta)$

Q5. Find dy/dx of following

- a) $x^p \cdot y^q = (x + y)^{p+q}$
- b) $y = x^x + x^{\sqrt{x}}$
- c) $x^y = e^{x-y}$

Q6. Find dy/dx of following

- a) $y = x^2 * e^{3x}$
- b) $y = \sin x * \cos(2x)$
- c) $y = e^{2x} \cdot \log(x + 1)$
- d) $y = e^x \cdot \sin^{-1} x$
- e) $y = (x^2 + 1)^5$
- f) $y = e^{x \cdot \log_e 5}$
- g) $y = e^{3x} \cdot \cos^{-1} 5x$
- h) $y = \log(x^2 + 2x + 5)$
- i) $y = \log_{20} x + 30^x$
- j) $y = (x^4 + 2x)^3 \cdot \sin(3x)$
- k) $x^2 + xy = y^3$
- l) $y = (\sin^{-1} x)^x + (\cos x)^{\sin x}$
- m) $4x^6 + 5x^2y^3 - 6y^4 = 0$
- n) Find $\frac{dy}{dx}$ if $x^2 + y^2 + xy - y$ at (1,2)
- o) Find $\frac{dy}{dx}$ if $13x^2 + 2yx^2 + y^3 = 1$

Topic: Application of Derivative

Q1. Find Tangent & normal equation for

- $2x^2 - xy + 3y^2 = 16$ at (3,1)
- $y = x^3 + 3x^2 - 9x + 7$ at (1, 2)
- $4x^2 + 9y^2 = 40$ at (1, 2)
- Find Equation of tangent & normal to curve $4x^2 + 9y^2 = 40$ at (3,2)
- Find equation of tangent and normal to curve $x = \frac{1}{t}, y = 1 - \frac{1}{t}$, if $t = 2$
- Slope of curve $2y^3 = ax^2 + b$ at (1,-1) is same as slope of $x + y = 0$
Find a & b.
- Find equations of tangent & normal to curve $2x^2 - xy + 3y^2 = 18$ at (3,1)
- Find two equation of tangent to curve $x^2 + y^2 + 6x - 6y - 7 = 0$ where it cuts X - axis.

Q2. Find Radius of curvature for

- To Curve $y = x^5$ at (3,-3)
- To Curve $y = 2 \sin x - \sin 2x$ at $x = \frac{\pi}{2}$
- To Curve $y = e^x$ at (0,1)
- To Curve $y = x(x - 2)$ at (2,0)
- To Curve $xy = c$ at point (c,c)
- To Curve $y = x^3$ at (2,8)
- To Curve $x^4 + y^4 = 2$ at (1,1)
- To curve $\sqrt{x} + \sqrt{y} = 1$ at $(\frac{1}{4}, \frac{1}{4})$
- To curve $y^2 = 4ax$ at (a,2a)

Q3. Find maxima and minima for

- $y = 2x^3 - 3x^2 - 36x + 10$
- $y = x^3 + 3x^2 - 2$
- $y = x^3 - 9x^2 + 24x$
- $y = x^3 - 18x^2 + 96x$

Q4. Solve

- Find dimension of rectangle of largest area having fixed perimeter 80cm.
- A metal wire 100cm long is bent to form a rectangle. Find side when area is max.
- Divide 120 in two parts such way that their product is maximum.
- Divide 20 in two parts such that product of one and cube of other is maximum.
- A manufacturer can sell x items at price Rs. $(330 - X)$ each. The cost of producing x items is Rs. $(X^2 + 10X + 12)$ Determine number of items to be sold so that manufacturer can make maximum profit.
- A manufacturer can sell ' x ' items per week at price $(23 - 0.001x)$ rupees each. It cost $(5x + 2000)$ rupees to produce x items. Find number of items to be produced per week for maximum profit.

Topic: Integration

For 2 Marks

a) $I = \int \log x \cdot dx$	b) $I = \int x \cdot e^x dx$	c) $I = \int \frac{1}{3x+5} dx$
d) $I = \int \cos 2x dx$	e) $I = \int (\cos x)^2 dx$	f) $I = \int (\tan x + \cot x)^2 dx$
g) $I = \int (\sin x)^2 dx$	h) $I = \int \sin 2x dx$	i) $I = \int (e^{3x} + a^{2x} + x^{4a} + a^{5a}) dx$

Q2. Solve

- a) $I = \int \frac{1}{2x+5} dx$
- b) $I = \int \frac{x}{x^2+6} dx$
- c) $I = \int 2\sqrt{x} dx$
- d) $I = \int (\sqrt{x} - x^2) dx$
- e) $\int \frac{1}{2x^2+3x+1} dx$
- f) $\int \frac{1}{(x+4)(x+9)} dx$
- g) $\int \frac{1}{(2-x)(2x-1)} dx$

Q2. Solve

- a) $I = \int x \cdot (\sin^{-1} x) dx$
- a) $I = \int x^3 \cdot (\tan^{-1} 4x) dx$
- b) $I = \int e^x \cdot \sin 4x dx$

Q3. Solve

- a) $I = \int \frac{x-3}{x^3-3x^2-16x+48} dx$
- b) $I = \int \frac{1}{2x^2+3x+1} dx$

Q4. Solve

- a) $I = \int \frac{e^x}{(e^x-1)(e^x+1)} dx$
- b) $I = \int \frac{1}{x(2-\log x)(2 \log x-1)} dx$

Topic: Numerical Method

Q1. Solve Using Gauss Elimination Method

- a) $x + y + z = 6, 3x - y + 3z = 10, 5x + 5y - 4z = 3$
- b) $x + y + z = 4, 2x + y + z = 5, 3x + 2y + z = 7$
- c) $x + y + z = 9, x - 2y + 3z = 8, x - y + 2z = 7$

Q2. Solve Using Newton Raphson Method 4 Iterations

- a) Find Cube root of 400
- b) $x^4 - x - 10 = 0$
- c) $x^3 - 2x - 5 = 0$

Q3. Solve Using Jacobi Method 3 Iterations

- a) $5x - y = 9, x - 5y + z = -4, y - 5z = 6$
- b) $x + y + 2z = 13, x + y - z = 1, x + 3y - z = 7$
- c) $10x - 2y - 2z = 6, -x - y + 10z = 8, -x + 10y - 2z = 7$

Q4. Solve Using Gauss – Seidel Method 3 Iterations

- a) $5x - y = 9, x - 5y + z = -4, y - 5z = 6$
- b) $x + y + 2z = 13, x + y - z = 1, x + 3y - z = 7$
- c) $10x - 2y - 2z = 6, -x - y + 10z = 8, -x + 10y - 2z = 7$